

- 1 The surface area of sphere **A** is nine times the surface area of sphere **B**

The difference between the volume of sphere **A** and the volume of sphere **B** is $117\pi \text{ cm}^3$

Find the radius of the smaller sphere.

Show your working clearly.

$$\text{area} : A : B = 9 \times \cancel{4\pi r^2} : \cancel{4\pi r^2} \quad (1)$$

$$\begin{aligned} \text{scale factor of radius} : A : B &= \sqrt{9} : 1 \\ &= 3 : 1 \quad (1) \end{aligned}$$

$$\text{difference in volume} : \frac{4}{3}\pi(3r)^3 - \frac{4}{3}\pi r^3 = 117\pi \quad (1)$$

$$\frac{4}{3}\pi(27r^3 - r^3) = 117\pi$$

$$26r^3 = \frac{117\pi}{\frac{4}{3}\pi}$$

$$26r^3 = 87.75$$

$$r^3 = \frac{87.75}{26} = 3.375$$

$$r = \sqrt[3]{3.375} \quad (1)$$

$$= 1.5 \quad (1)$$

1.5

..... cm

(Total for Question 1 is 5 marks)